



$$\cos(2n+1)\theta = \cos \theta - 2 \sin \theta \sum_{k=1}^n \sin 2k\theta$$

$$\sum_{k=1}^n \sin 2k\theta = \frac{\cos \theta}{2 \sin \theta} - \frac{\cos(2n+1)\theta}{2 \sin \theta} = \frac{1}{2} \cot \theta - \frac{\cos(2n+1)\theta}{2 \sin \theta}$$